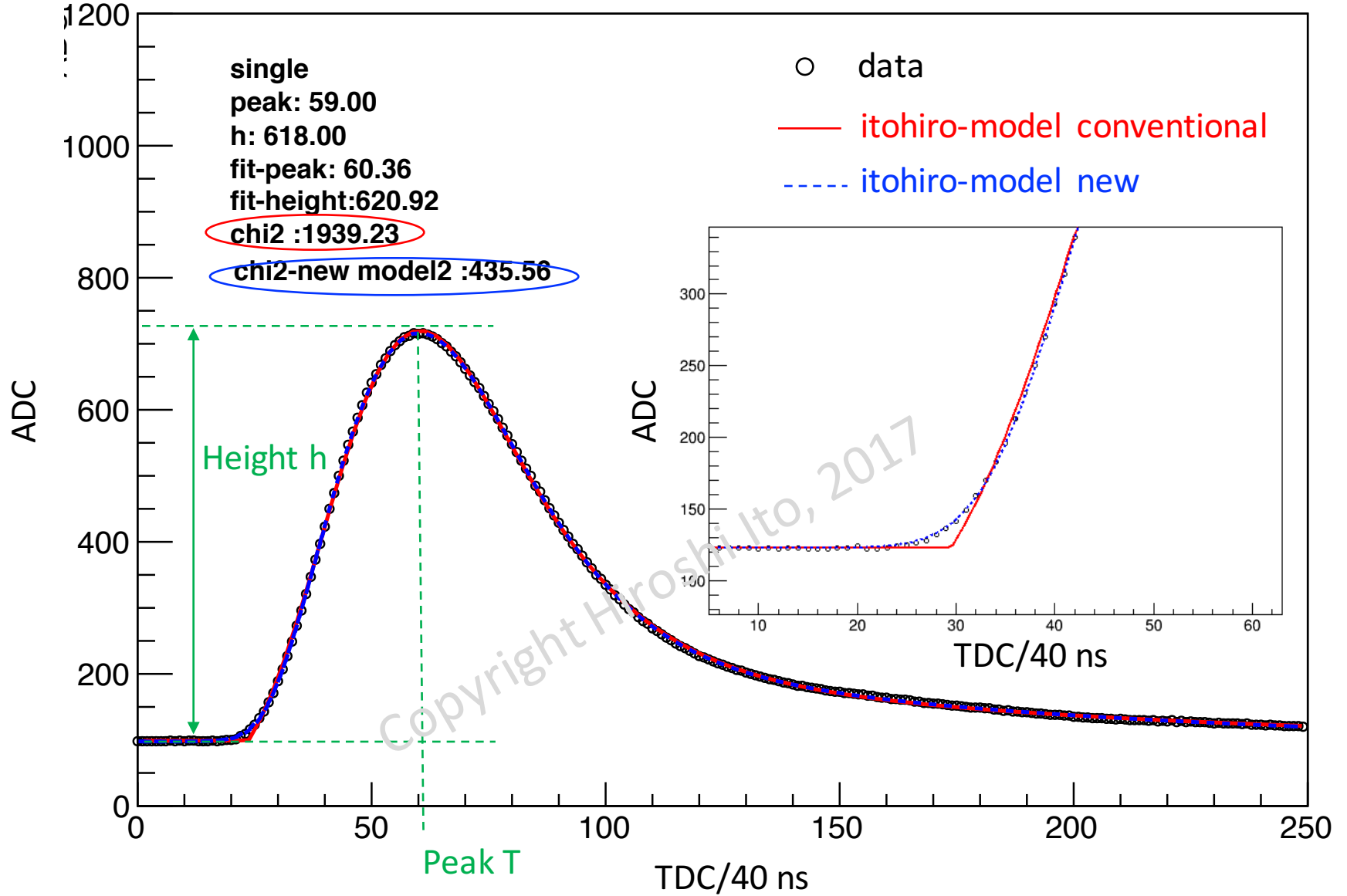


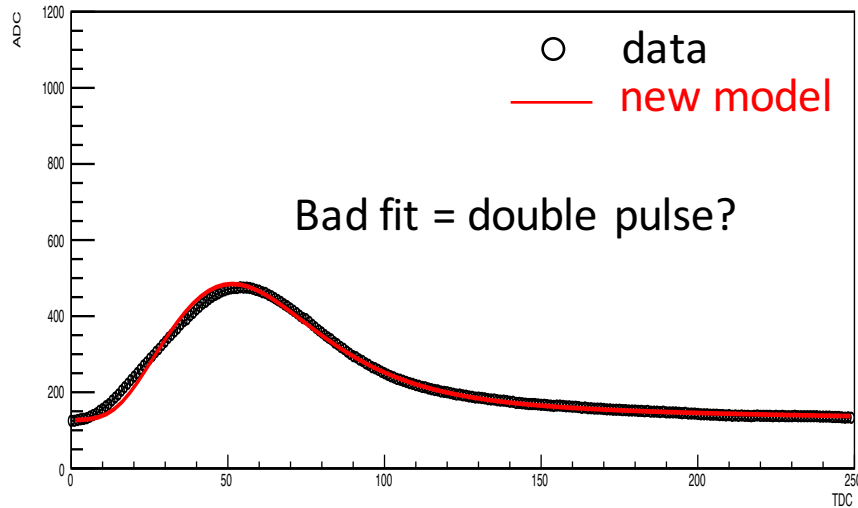
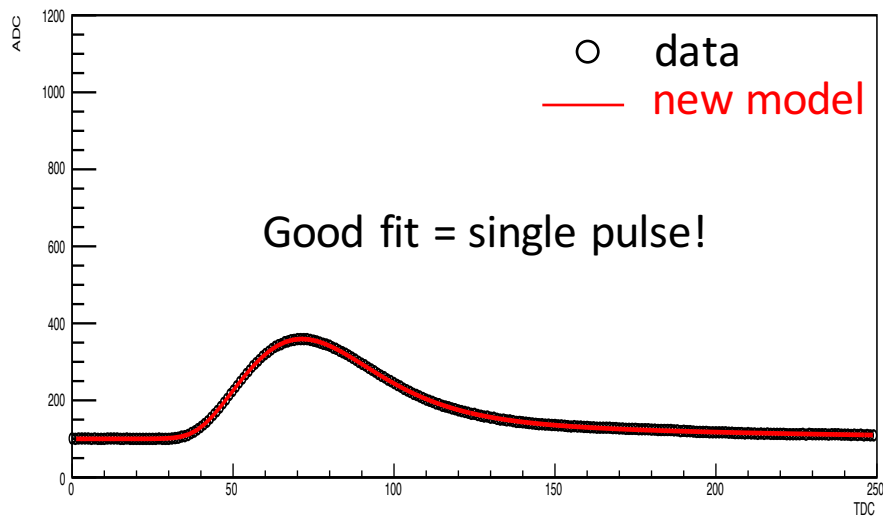
CsI(Tl) Waveform Model Development

Hiroshi Ito
Chiba Univ.

CsI(Tl) Waveform Fitting



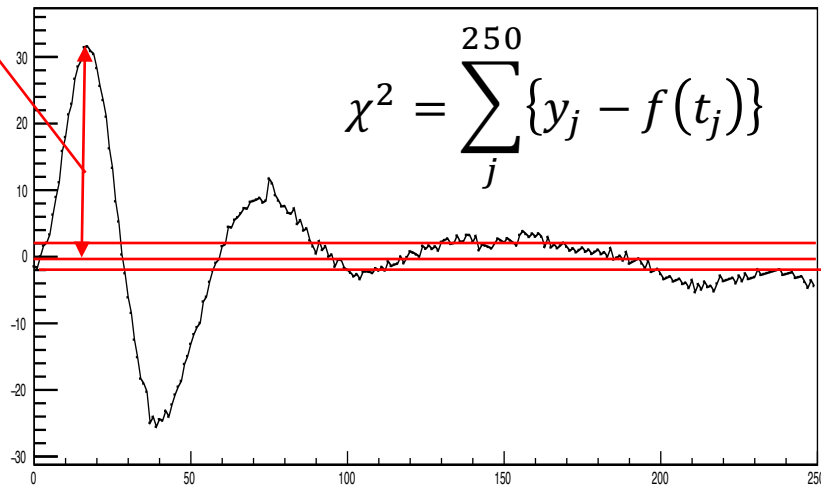
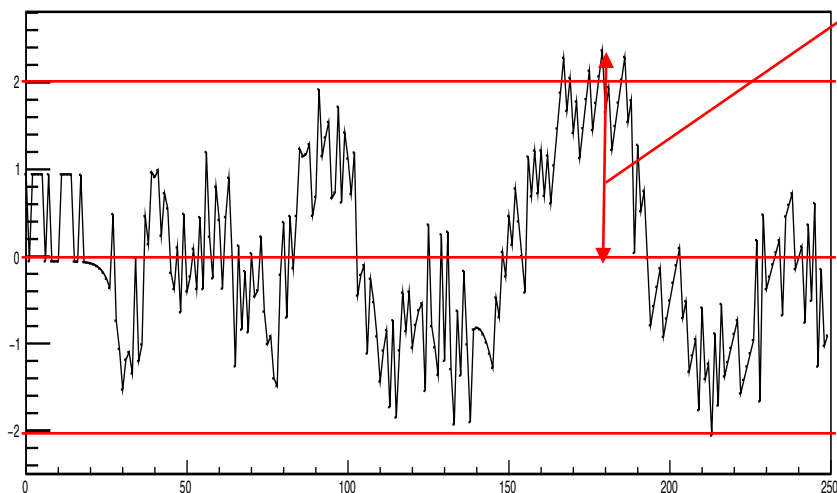
Deviation with the fitting function and data



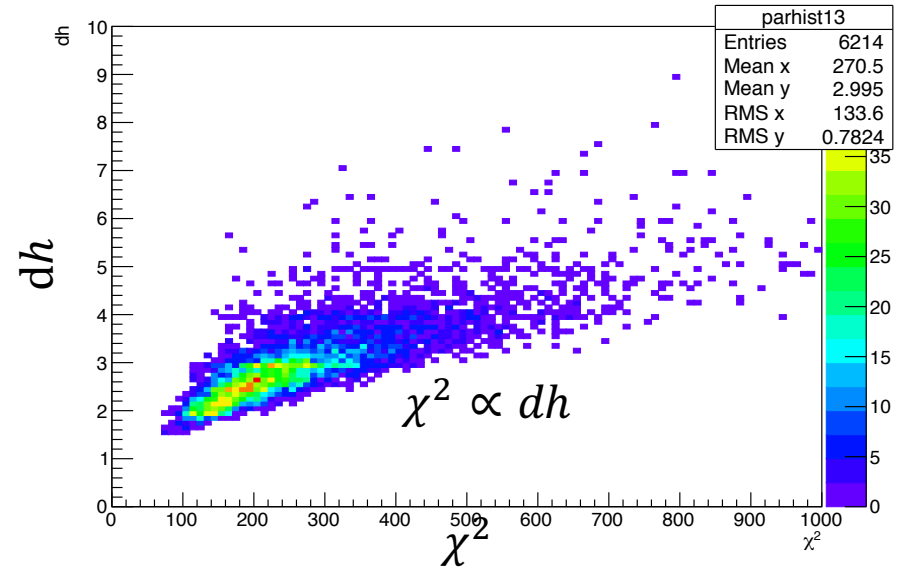
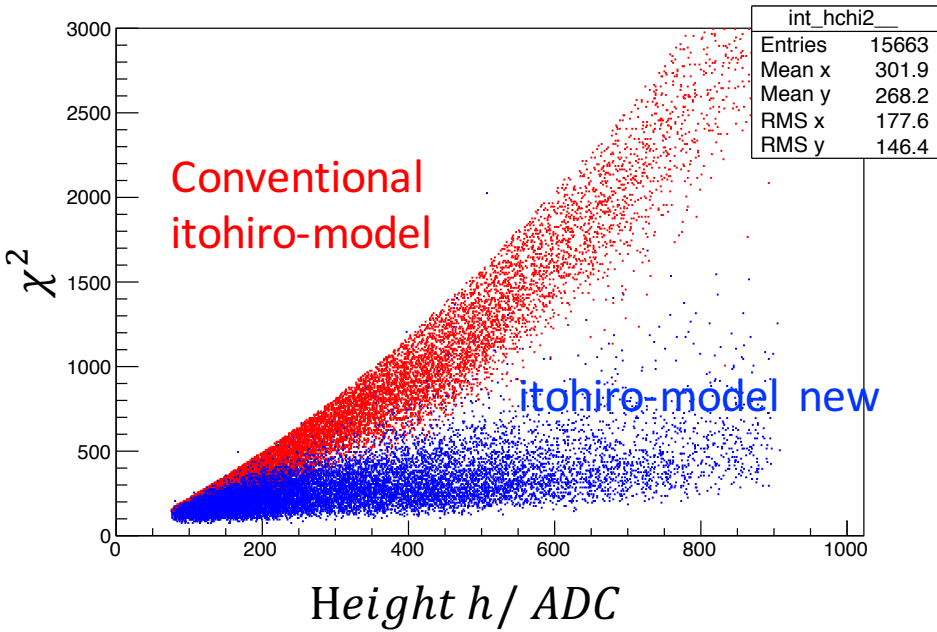
Graph

dh=max deviation

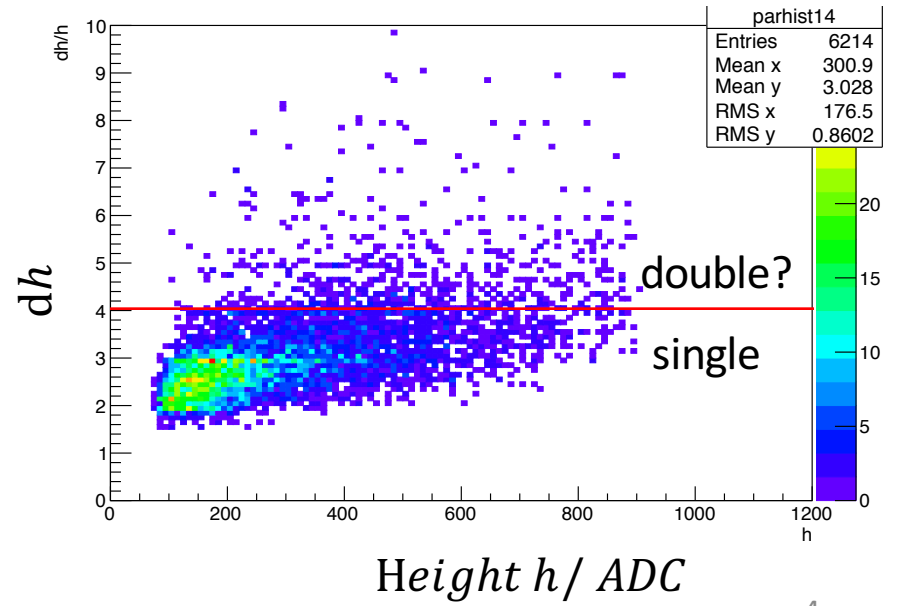
Graph



Single Pulse by Conventional Model



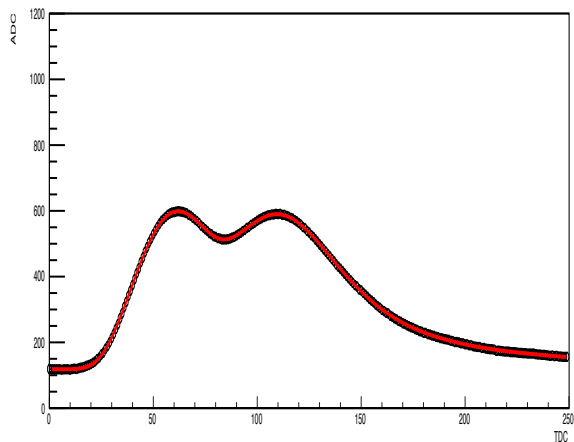
double pulse threshold
 $dh > 4$



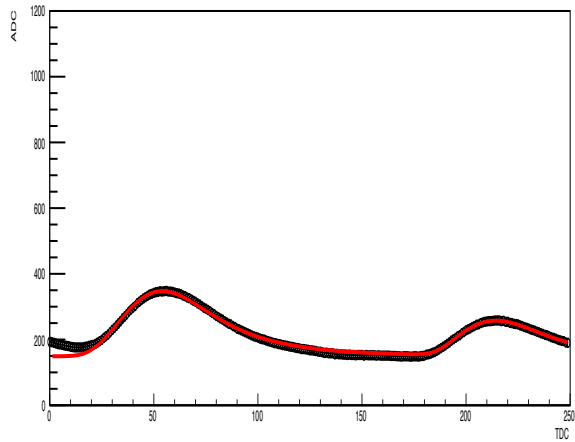
Double pulse Fitting

Waveform

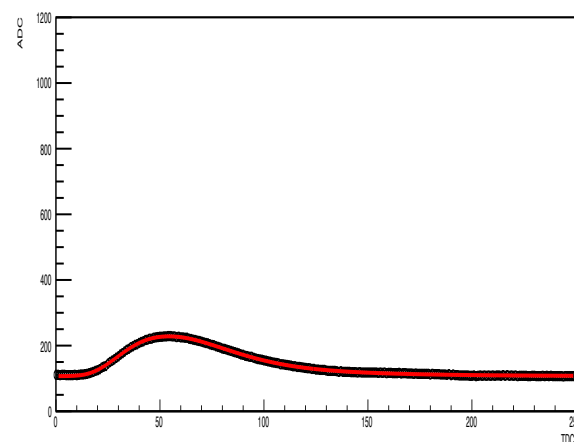
(run,n,x,y)=(3994,2,2,16)



(run,n,x,y)=(3994,2,13,27)

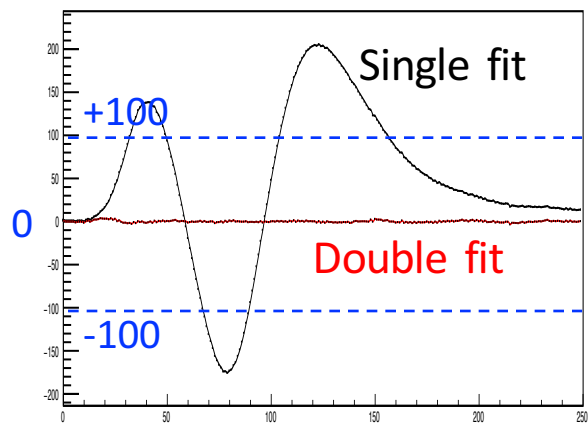


(run,n,x,y)=(3994,2,8,31)

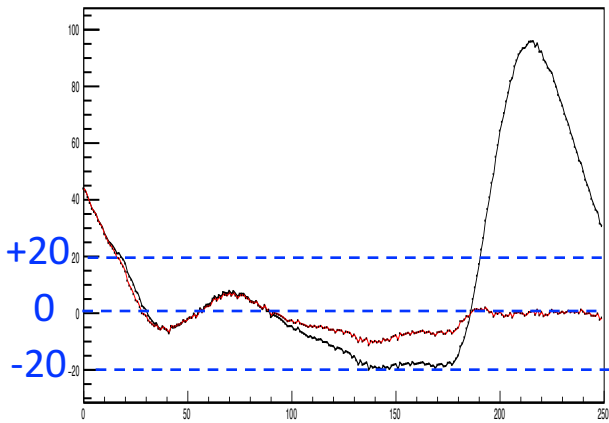


Deviation

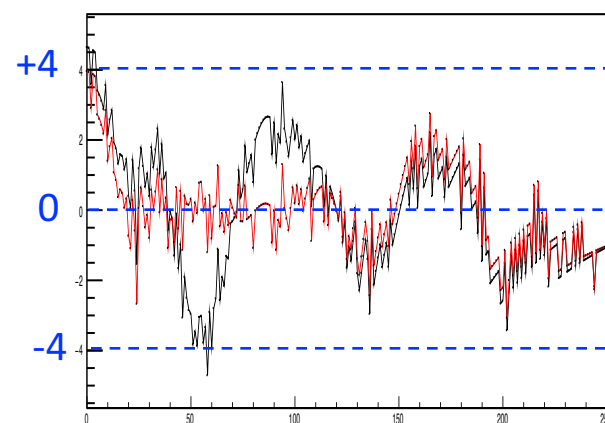
Graph



Graph



Graph

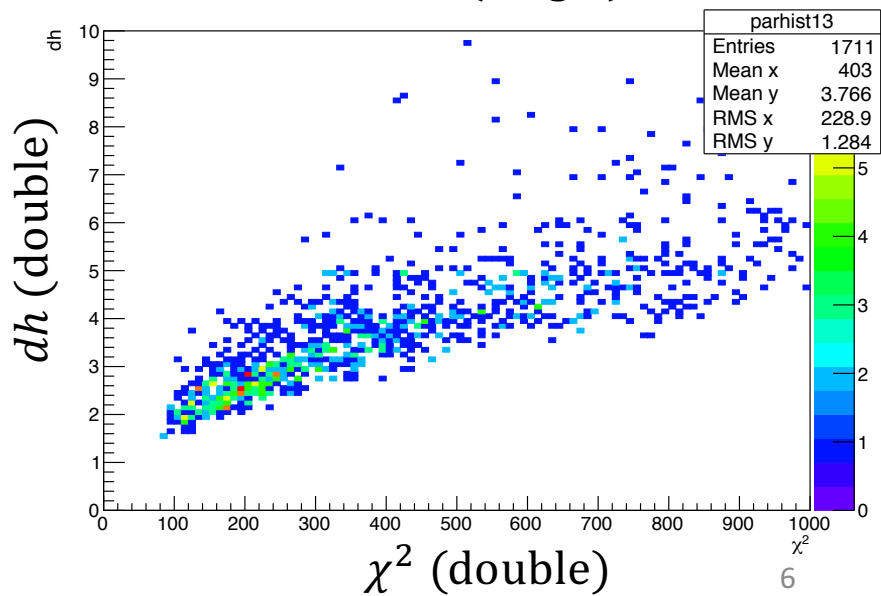
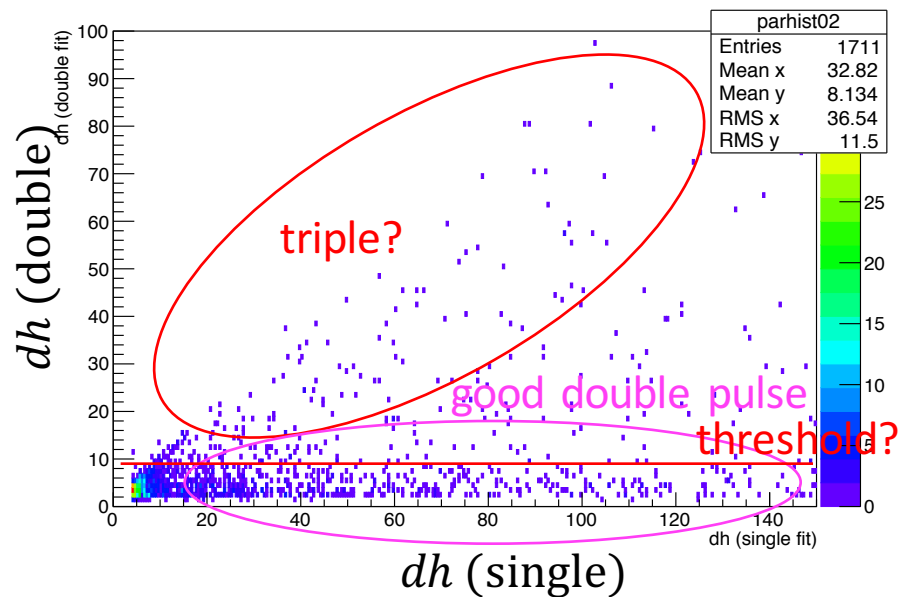
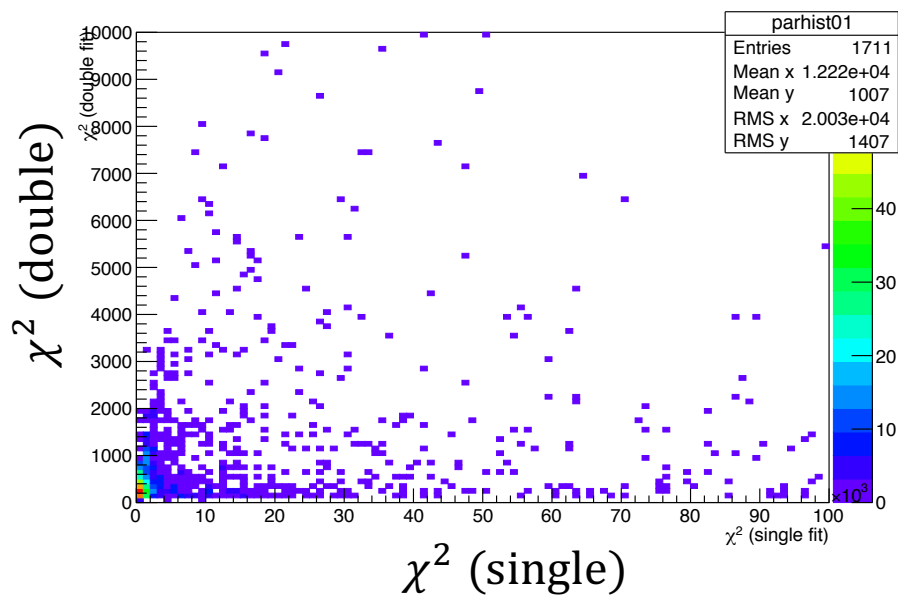


Single fit \times
 Double fit \bigcirc
 \Rightarrow Double pulse

Single fit \times
 Double fit \times
 $T \Rightarrow$ ripple pulse

Single fit \triangle
 Double fit \triangle
 \Rightarrow Single pulse?

New Model Fitting function



Summary

- New waveform model was developed, its χ^2 is lower than conventional model.
- The new model has not stepping term.
- Good fit can be identified by determination as max of the deviation (dh) less than 4.
- The model was imported to KEKCC based Fortran.
- Time resolution and energy calibration will be performed for new model.

Backup

New Model Fitting function

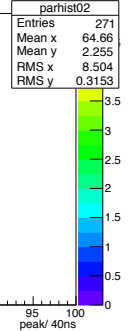
$$F(t) = \frac{A}{1 - \exp\left(-\frac{t - t_0}{\lambda}\right)} \cdot \text{Freq}\left(\frac{t - t_0 - d}{\mu}\right)$$

$$\left\{ \frac{t - t_0}{\tau_1} \exp\left(1 - \frac{t - t_0}{\tau_1}\right) + \varepsilon \frac{t - t_0}{\tau_2} \exp\left(1 - \frac{t - t_0}{\tau_2}\right) \right\}$$

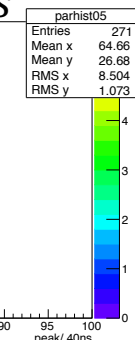
λ

d

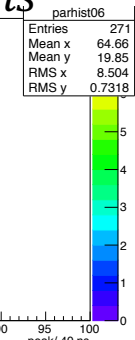
μ



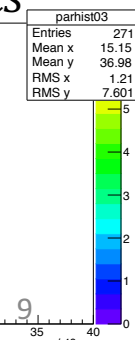
Peak T / 40 ns



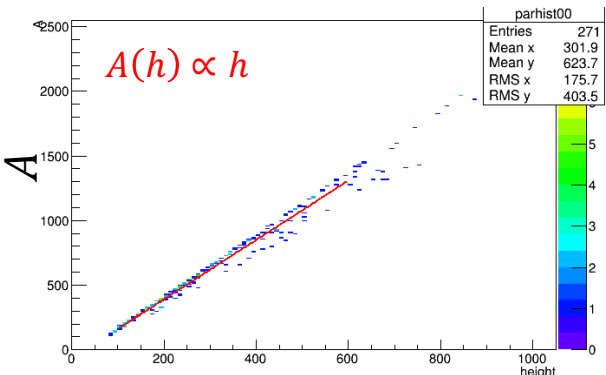
Peak T / 40 ns



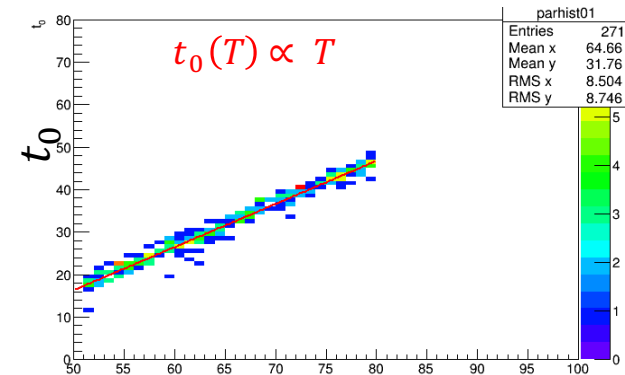
Peak T / 40 ns



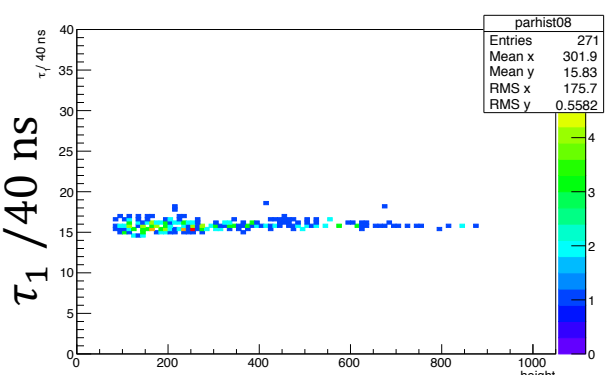
Peak T / 40 ns



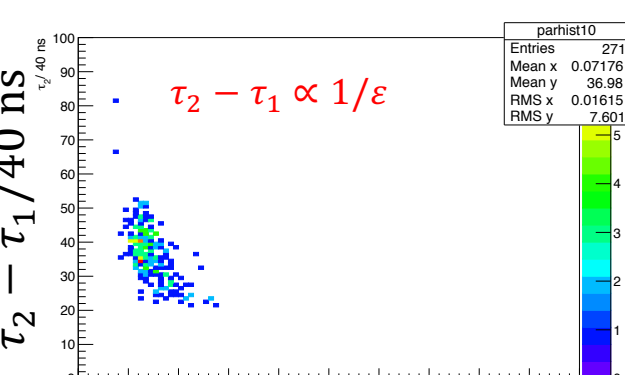
Height h / ADC



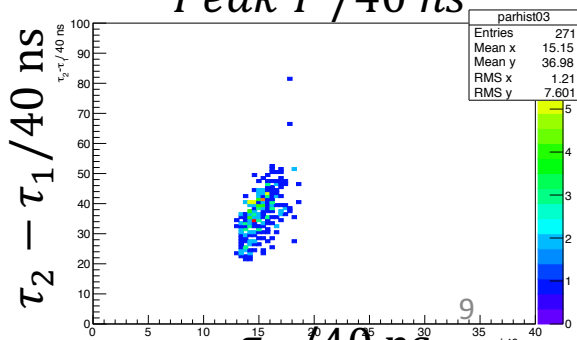
Peak T / 40 ns



Height h / ADC



ε



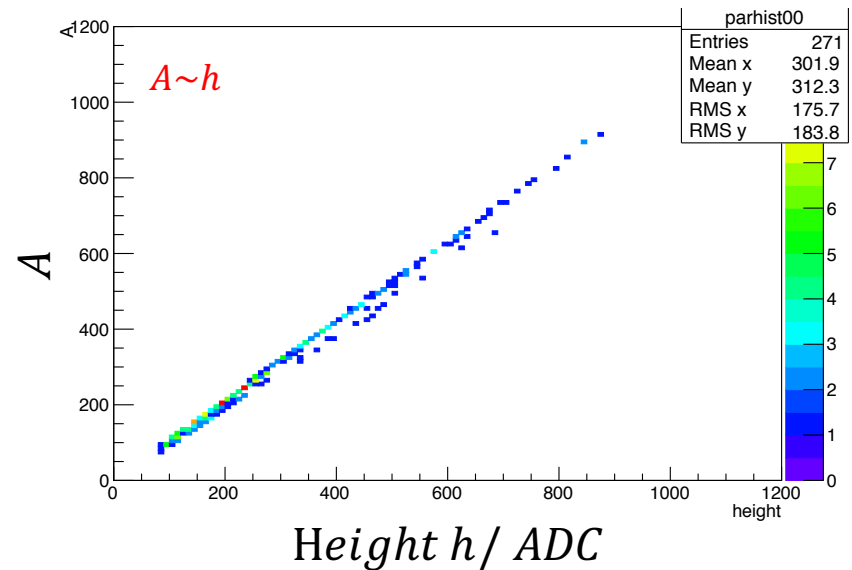
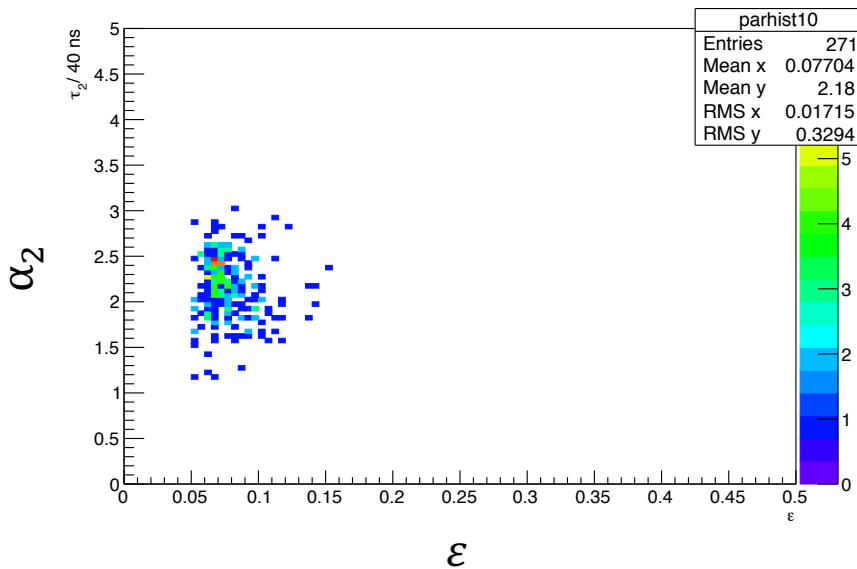
2017/08/04

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New Model Fitting function

$$F(t) = \frac{\tilde{A}(A, h)}{1 - \exp\left(-\frac{t - t_0(T)}{\lambda}\right)} \cdot \text{Freq}\left(\frac{t - t_0(T) - d}{\mu}\right) \cdot \left\{ \frac{t - t_0(T)}{\tau_1} \exp\left(1 - \frac{t - t_0(T)}{\tau_1}\right) + \varepsilon \frac{t - t_0(T)}{\tau_2(\varepsilon, \alpha_2)} \exp\left(1 - \frac{t - t_0(T)}{\tau_2(\varepsilon, \alpha_2)}\right) \right\}$$

$$\text{Freq}(x) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^x \exp(-t^2/2) dt$$



$$F(t) = \frac{A}{1 - \exp\left(-\frac{t-t_0}{\lambda}\right)} \cdot \text{Freq}\left(\frac{t-t_0-d}{\mu}\right) \cdot \left\{ \frac{t-t_0}{\tau_1} \exp\left(1 - \frac{t-t_0}{\tau_1}\right) + \varepsilon \frac{t-t_0}{\tau_2} \exp\left(1 - \frac{t-t_0}{\tau_2}\right) \right\}$$

$t=t_0$ の場合の発散問題

$$\frac{t-t_0}{1 - \exp\left(-\frac{t-t_0}{\lambda}\right)}$$

$$\begin{aligned} \frac{x}{1 - e^x} &= \frac{x}{1 - \left\{1 - x + \frac{x^2}{2!} - \frac{x^3}{3!}\right\}} \\ &= 1 \end{aligned}$$